

Stochastic differential equations with multiple timescales

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Plan

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 - Concentration results
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5. Some applications
 - Van der Pol oscillator
 - Excitability
 - Folded-node singularity, canards

Bibliography

General references

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Introduction and overview articles

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